

SDSS-IV MaNGA: stellar population gradients within barred galaxies

Amelia Fraser-McKelvie¹,¹★ Michael Merrifield,¹ Alfonso Aragón-Salamanca¹,¹
 Thomas Peterken,¹ Karen Masters^{2,3}, Coleman Krawczyk,³ Brett Andrews,⁴
 Johan H. Knapen,^{5,6,7} Sandor Kruk⁸, Adam Schaefer,⁹ Rebecca Smethurst⁸,
 Rogério Riffel^{10,11}, Joel Brownstein¹² and Niv Drory¹³

¹*School of Physics & Astronomy, University of Nottingham, University Park, Nottingham NG7 2RD, UK*

²*Department of Physics and Astronomy, Haverford College, 370 Lancaster Ave, Haverford, PA 19041, USA*

³*Institute of Cosmology & Gravitation, University of Portsmouth, Dennis Sciama Building, Portsmouth PO1 3FX, UK*

⁴*PITT PACC, Department of Physics and Astronomy, University of Pittsburgh, Pittsburgh, PA 15260, USA*

⁵*Instituto de Astrofísica de Canarias, E-38205 La Laguna, Tenerife, Spain*

⁶*Departamento de Astrofísica, Universidad de La Laguna, E-38205 La Laguna, Tenerife, Spain*

⁷*Astrophysics Research Institute, Liverpool John Moores University, IC2, Liverpool Science Park, 146 Brownlow Hill, Liverpool L3 5RF, UK*

⁸*Department of Astrophysics, University of Oxford, Denys Wilkinson Building, Keble Road, Oxford OX1 3RH, UK*

⁹*Department of Astronomy, University of Wisconsin-Madison, 475N. Charter St, Madison, WI 53703, USA*

¹⁰*Departamento de Astronomia, IF, Universidade Federal do Rio Grande do Sul, CP 15051, 91501-970, Porto Alegre, RS, Brazil*

¹¹*Laboratório Interinstitucional de e-Astronomia, Rua General José Cristino, 77 Vasco da Gama, Rio de Janeiro 20921-400, Brazil*

¹²*Department of Physics and Astronomy, University of Utah, 115 S. 1400 E., Salt Lake City, UT 84112, USA*

¹³*McDonald Observatory, The University of Texas at Austin, 1 University Station, Austin, TX 78712, USA*

Accepted 2019 May 31. Received 2019 May 20; in original form 2019 April 10

ABSTRACT

Bars in galaxies are thought to stimulate both inflow of material and radial mixing along them. Observational evidence for this mixing has been inconclusive so far, however, limiting the evaluation of the impact of bars on galaxy evolution. We now use results from the MaNGA integral field spectroscopic survey to characterize radial stellar age and metallicity gradients along the bar and outside the bar in 128 strongly barred galaxies. We find that age and metallicity gradients are flatter in the barred regions of almost all barred galaxies when compared to corresponding disc regions at the same radii. Our results re-emphasize the key fact that by azimuthally averaging integral field spectroscopic data one loses important information from non-axisymmetric galaxy components such as bars and spiral arms. We interpret our results as observational evidence that bars are radially mixing material in galaxies of all stellar masses, and for all bar morphologies and evolutionary stages.

Key words: galaxies: evolution – galaxies: general – galaxies: spiral – galaxies: stellar content.

1 INTRODUCTION

Galactic bars are long-lived phenomena (Gadotti et al. 2015) that occur in a large fraction of local Universe disc galaxies (e.g. Knapen, Shlosman & Peletier 2000; Masters et al. 2011). Simulations show gas and angular momentum may be funnelled along bars to the central regions of a galaxy (e.g. Simkin, Su & Schwarz 1980; Weinberg 1985; Knapen et al. 1995; Minchev & Famaey 2010; Brunetti, Chiappini & Pfenniger 2011; Spinoso et al. 2017), and bar-driven secular evolution is a likely candidate for the cessation

of star formation in galaxies at late times (e.g. Masters et al. 2012; Kruk et al. 2018).

The orbits of stars within bars have been well studied (e.g. Combes & Sanders 1981; Sellwood 1981; Athanassoula 1992). The classical picture of bar formation and evolution requires the majority of stars in bar regions to be trapped around periodic elongated orbits in the direction of the bar major axis, known as the x_1 class of orbits (Contopoulos & Papayannopoulos 1980). If we assume that bar stellar orbits are indeed elongated with respect to stellar orbits within the disc of the galaxy, the bar may be treated as a confined structure within a galaxy. It follows that we would expect a greater radial mixing of stellar populations within bars if they formed from the same population as the disc. This would

★ E-mail: Amelia.Fraser-McKelvie@nottingham.ac.uk

manifest itself observationally as weaker stellar age and metallicity gradients within the bar regions compared to non-bar regions of the galaxy at the same radii. We will refer to this mixing of stellar populations within a bar as ‘radial mixing’, but note this is a separate phenomenon to the radial mixing observed in discs of barred galaxies outside co-rotation, as described in previous literature (e.g. Friedli, Benz & Kennicutt 1994; Di Matteo et al. 2013).

Observations of the direct effect of a bar on its host galaxy have been diverse in their approach, and have produced contrasting results. Single-fibre studies of the stellar populations of central (bulge-dominated) regions of barred galaxies have been shown to be no different to those of non-barred galaxies (Cacho et al. 2014). In addition, azimuthally averaged gradients over inner regions are also comparable to non-barred galaxies (Cheung et al. 2015). Outside co-rotation, simulations predict a flattening of stellar population gradients (Friedli et al. 1994; Minchev & Famaey 2010) thought to be due to the resonant coupling between bars and spiral arms. This was not reproduced in observational results, however (Sánchez-Blázquez et al. 2014). It is possible that in averaging across an entire galaxy, any subtle difference in the stellar populations as a result of the presence of a bar is lost.

Recent long-slit and integral-field spectroscopic results have begun to extricate the bar component and attempt to treat it as a separate entity within a galaxy. Long-slit works such as those by Pérez, Sánchez-Blázquez & Zurita (2007) and Pérez, Sánchez-Blázquez & Zurita (2009) placed slits along the bar major axes of a small sample of galaxies, reporting differences in stellar population gradient trends. For a sample of 20 galaxies, the authors report bars can possess positive, negative, or no metallicity gradient, and these gradients are correlated with galaxy velocity dispersion and mean stellar age. Sánchez-Blázquez et al. (2011) reanalysed the observations of Pérez et al. (2009) to include the disc regions of two barred galaxies, and found the bars of these galaxies contained flatter age and metallicity gradients. In a novel approach, Williams, Bureau & Kuntschner (2012) measure stellar population gradients of the central regions of 22 edge-on disc galaxies with boxy-peanut bulges (indicating the presence of a bar), and find flattened stellar population gradients when compared to non-barred galaxies. It seems that spatial information is crucial in determining stellar population trends across galaxies that contain non-axisymmetric structures. Indeed, when spatially resolved integral field spectroscopy is considered, Seidel et al. (2016) in a pilot study confirm a telltale flattening of stellar metallicity gradients on average along bars compared to disc regions of the same galaxy in 16 galaxies. The above results are consistent with bar mixing, though all have been derived from studies of small samples of galaxies. Whether this trend holds for all barred galaxies, and through all stages of bar evolution, is not known.

It is clear that in order to facilitate a detailed analysis of stellar population gradient trends, a large sample of barred galaxies, spatially resolved spectroscopy, and bar positional information within the galaxy are required. All three of these conditions are met by using the Mapping Nearby Galaxies at APO (MaNGA) galaxy survey in conjunction with the new citizen science project, Galaxy Zoo:3D, which aims to separate light from structural galaxy components within MaNGA data cubes. With this in mind, in this letter we examine the stellar populations within the bar and disc regions of a large sample of local-Universe barred galaxies using integral field spectroscopic (IFS) data from the MaNGA galaxy survey. In Section 2, we describe the MaNGA survey and the barred galaxy sample used, in Section 3 we detail how the stellar

population indicators are measured, and in Section 4 we present the results.

2 SAMPLE

2.1 The MaNGA Galaxy Survey

The MaNGA Galaxy Survey is an IFS survey that aims to observe 10 000 galaxies by 2020 (Bundy et al. 2015; Drory et al. 2015). It is an SDSS-IV project (Blanton et al. 2017), employing the 2.5 m telescope at Apache Point Observatory (Gunn et al. 2006) and BOSS spectrographs (Smee et al. 2013). MaNGA Product Launch 7 (MPL-7) contains 4620 unique galaxy observations, observed and reduced by the MaNGA Data Reduction Pipeline (Law et al. 2016), with derived properties produced by the MaNGA data analysis pipeline (DAP; Westfall et al. 2019), provided as a single data cube per galaxy (Yan et al. 2016a). MaNGA’s target galaxies were chosen to include a wide range of galaxy masses and colours, over the redshift range $0.01 < z < 0.15$, and the Primary+ sample (Yan et al. 2016b; Wake et al. 2017) contains spatial coverage out to $\sim 1.5 R_e$ for ~ 66 per cent of all observed galaxies.

2.2 Barred galaxy sample

We select barred galaxies within the MaNGA MPL-7 sample using Galaxy Zoo 2 (Hart et al. 2016), which is a citizen science project that provides morphological classifications for all MaNGA galaxies. We select galaxies with a weighted bar vote fraction of > 0.7 , which is the fraction of respondents that classified a particular galaxy as possessing a bar, weighted by participant agreement level with other users. From the 4620 galaxies in MPL-7, 488 are thus classified as highly likely to contain bars. We note that this is ~ 10 per cent of the original sample, and that while we are confident we have selected barred galaxies, these will be the strongest barred galaxies in the MaNGA sample.

Apart from determining whether a galaxy possesses a bar, for spatially resolved stellar population analysis of a large sample of galaxies, we also require an automated method to determine the region in the IFS datacube where the bar lies. For this, we use Galaxy Zoo:3D (GZ:3D; Masters et al. in preparation), a new citizen science project that asks participants to trace regions on a galaxy image that correspond to various components seen, including bars, spiral arms, and bulges. The regions drawn are translated into masks, weighted by the number of users that determined each spatial pixel (spaxel) to be located within the region of interest. Fig. 1 shows an example of the GZ:3D masks for the MaNGA galaxy 8451-6101.

The initial input sample into GZ:3D was galaxies that were likely to contain spiral arms according to Galaxy Zoo 2 from MPL-5 (2836 galaxies). While not all of these galaxies actually contain spiral arms, the large majority do, and hence our sample is biased towards spiral galaxies, with less than 15 per cent S0s. To date, GZ:3D has only been run on a portion of the MaNGA sample, and of the 488 barred galaxies in MPL-7, 128 also possess GZ:3D bar region masks. This final sample of 128 barred galaxies spans a mass range of $5.3 \times 10^8 < M/M_\odot < 1.4 \times 10^{11}$. There is a slight bias in the sample used in this analysis towards lower mass, optically bluer galaxies than the overall barred galaxy population in MaNGA (a result of the low S0 fraction that possess GZ:3D masks), but differences in median colour and mass distributions are less than 1σ .

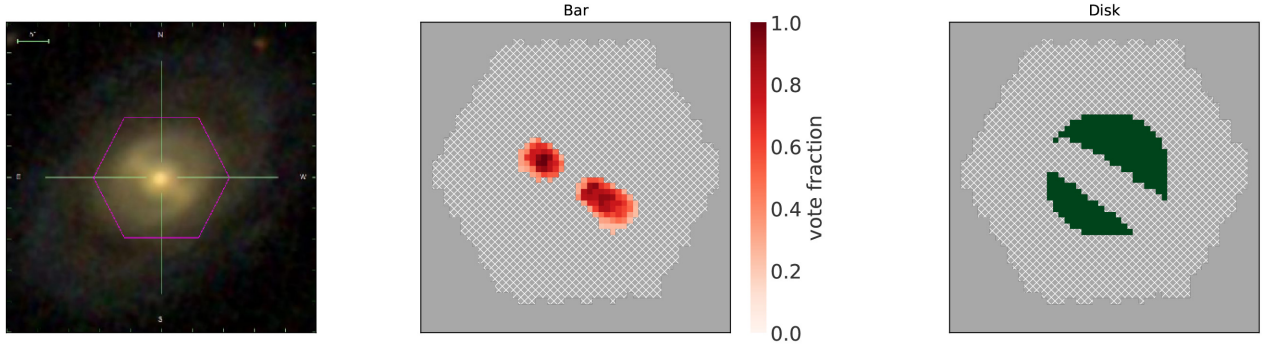


Figure 1. The barred galaxy 8451-6101 (left, with MaNGA field of view as the pink hexagon), and its Galaxy Zoo:3D bar (red, centre) and disc (green, right) masks. The bar mask is scaled by the total vote fraction of respondents. Only spaxels with a vote fraction greater than 0.2 are included in the bar region for analysis. We exclude the central region of the galaxy in our gradient determination in order to compare bar and disc gradients at the same radii. The disc is defined as any spaxel within the IFU field of view that is not included in the bar region.

3 MEASURING STELLAR POPULATIONS

In order to compare the physical properties both within and outside the bar for a given radius, we extract the stellar populations of both the bar and disc regions of barred MaNGA galaxies using full spectral fitting. As a check, we also derive population properties from index measurements. We define the bar regions as any spaxel within the GZ:3D bar masks in which at least 80 percent of respondents have determined this to be a bar region. We make this conservative cut to account for any respondents who drew spurious regions on the GZ:3D images. We define a corresponding disc region as all spaxels within the same radius as the original bar masks, but not within the bar mask. We note that spiral arms generally exist outside a bar radius, and in the cases where they do contaminate our measured disc region, we ignore any secondary effects they may contribute for this analysis. It is important to compare regions within a galaxy at similar radii, and given our definition of the bar region, it is clear there are no associated disc regions in the central radii of a galaxy. For this reason, we exclude the central regions of the galaxy from this analysis, and choose only to look at regions of the galaxy that have both bar and disc spaxel mask regions. We note that stellar population gradients measured may differ from literature values as we are not including the central regions of the galaxy, but this ensures bar and disc stellar population parameters will be internally consistent with one another for a given galaxy.

We perform full spectral fitting using STARLIGHT (Cid Fernandes et al. 2005), and a subset of the E-MILES set of synthetic SSP templates (Vazdekis et al. 2016) on every spaxel in the MaNGA barred galaxy sample. We do not require spatial binning as we are rarely using spaxels in outer (lower signal-to-noise) regions of the IFUs, and need to avoid blending any signal into bins that incorporate both bar and disc regions. By assuming a Kroupa revised IMF (Kroupa 2001), BaSTI isochrones (Pietrinferni et al. 2004), and a Milky Way α/Fe , the best-fitting spectrum is obtained along with the weighted combination of templates used, from which we derive average ages and metallicities for each spaxel.

For the index-derived stellar population estimates, we employ $H\beta$ as a stellar age indicator, as it is sensitive to the presence of young stars, and $[\text{MgFe}]'$, defined by

$$[\text{MgFe}]' = \sqrt{(\text{Mgb}(0.72 \times \text{Fe5270} + 0.28 \times \text{Fe5335}))},$$

as a stellar metallicity indicator. Both these indices are relatively insensitive to changes in α/Fe ratio (González 1993). Using PPXF (Cappellari 2017), the MaNGA DAP fits a combination of stellar

spectra to the MaNGA spectrum, then subtracts emission lines, measures absorption lines, and corrects for instrumental resolution and Doppler broadening effects (Westfall et al. 2019). The resultant maps of absorption line indices are used in this work. We infer age and metallicity estimates from index measurements by interpolating over a grid of MILES SSP models of Vazdekis et al. (2010), scaled to the flux-weighted average velocity dispersion of the galaxy.

4 RESULTS AND DISCUSSION

To measure the stellar population gradients, we first average all spaxel age and metallicity values in azimuthal rings of 0.5 arcsec based on the light-weighted elliptical radius of each spaxel from the galaxy centre. This measurement takes into account inclination effects so that regions at the same physical radius from the centre of a galaxy are compared to each other. A linear least-squares fit was then performed to the STARLIGHT- and index-derived age and metallicity values as a function of their (linear) distance to the galaxy centre to obtain the age and metallicity gradients.

In Fig. 2, we present the bar and disc stellar population gradients for each galaxy in the sample, coloured by the galaxy's stellar mass, from STARLIGHT mass-weighted and light-weighted ages and metallicities, as well as the index-derived populations (which may be thought of as being closer to the STARLIGHT light-weighted output). Reassuringly, the full spectral fitting and index-derived outputs are consistent with each other. There is some scatter at the high-mass end of the $H\beta$ -derived age gradients, which is likely because of the difficulty in distinguishing beyond ages of ~ 5 Gyr using $H\beta$. We see that for both the age and metallicity indicators, on average, the magnitude of the gradient within the bar is significantly smaller than within the disc for all stellar masses. This is a strong indication that material is better radially mixed in the bar than within the surrounding regions. The line of best fit to the bar and disc gradients is shown in green, and the gradient, m , and 1σ error on this value printed at the top of each panel. In each case, the best-fitting line slope is significantly incompatible with a gradient of unity, typically by $> 5\sigma$, indicating that on average, the bar stellar population gradients are flatter than the disc measurements. From this, we conclude that bars are efficient at radially mixing material along themselves.

While on average the bar age and metallicity gradients are flatter within the bar than the corresponding disc region, we note that some galaxies (up to 29 percent of the sample for the STARLIGHT mass-weighted age gradients) actually possess disc gradients that

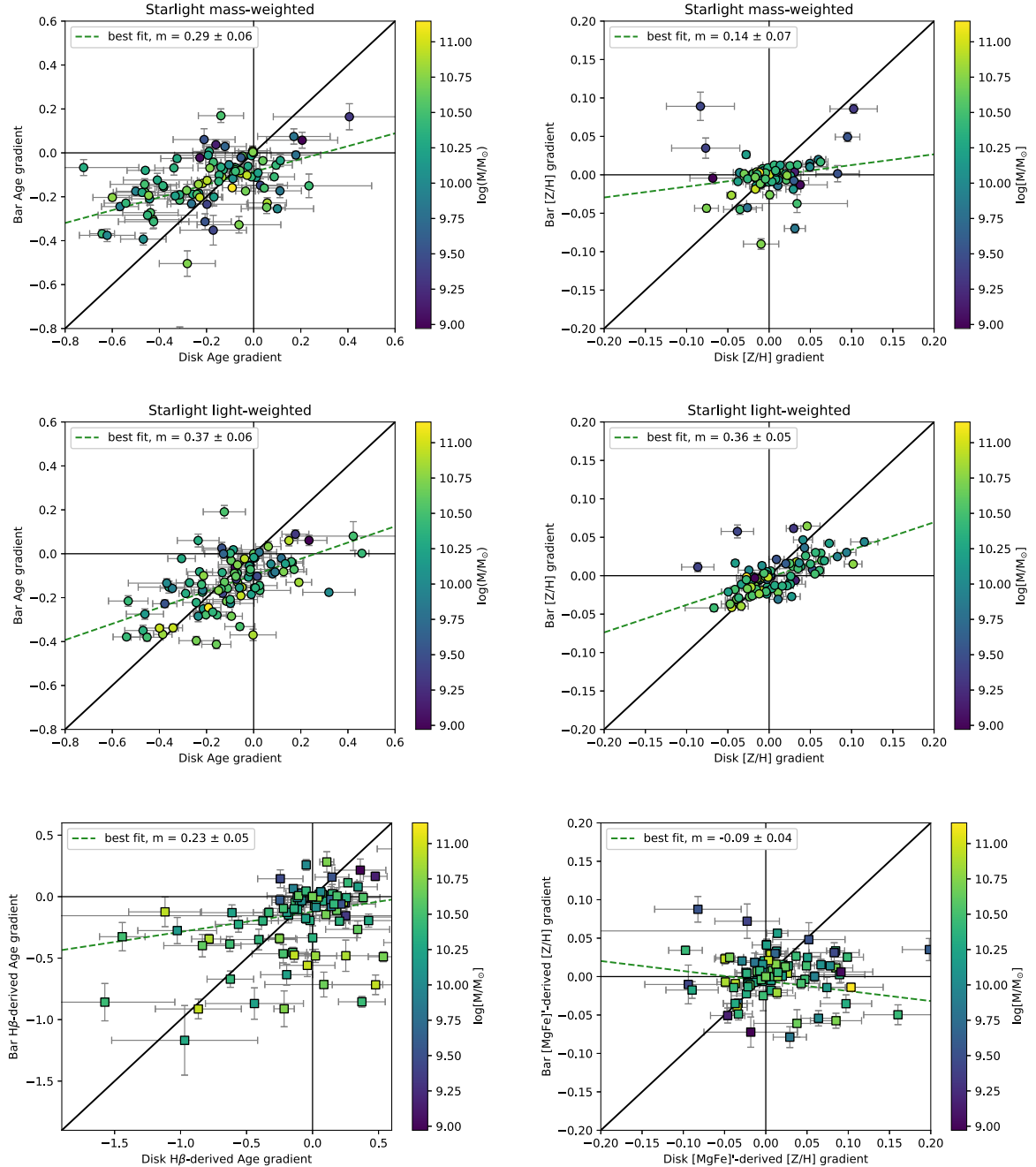


Figure 2. Bar and disc age (left-hand column) and metallicity (right-hand column) gradient comparisons for STARLIGHT mass-weighted (top row), light-weighted (middle row) full spectral fits, and the derived ages and metallicity gradients from index measurements (bottom row, the square markers, note different scale on H β -derived age plot). The black 1:1 lines denote where the bar and disc gradient is the same for a given galaxy, and a green dashed line indicates the best fit to the data points on each plot. In all cases, stellar population gradients are flatter within the bar than within the disc, indicating that bars are radially mixing stars.

are flatter than the bar gradients. While this may be mostly explained by scatter caused by the error in the gradient measurements, this is not correlated with stellar mass. Further work to determine whether bar parameters (such as bar length and strength, or age), or galactic parameters (such as environment) influence bar stellar population gradients are left for a future work. We also note the portion of galaxies that possess positive metallicity gradients. Given we are excluding the very central (bulge-dominated) regions from the gradient measurement, and only measuring along the length of the

bar (which is generally smaller than the radius of the galaxy), it is perhaps not surprising that gradient measurements are not all negative, and should not be compared to literature values for azimuthally averaged galaxies over the entire radial extent of the galaxy.

It seems that the bar regions of barred galaxies possess distinct stellar population gradients compared to regions outside the bar at the same radii. This agrees well with the results of Seidel et al. (2016), who report systematically flatter Fe5015 and Mg b gradients

along the bar major axis, compared to the bar minor axis for 16 barred galaxies. Seidel et al. (2016) showed that the gradients found along the minor axis of the inner regions of barred galaxies are frequently comparable to the inner regions of non-barred galaxies. From this, we conclude that bars are confined structures that may be considered as an individual component within a galaxy. Sánchez-Blázquez et al. (2011) find similar when examining the long-slit observations of Pérez et al. (2009) for two galaxies. We have shown that these trends hold robustly for a much larger sample of barred galaxies, and across a wide range of host galaxy stellar masses and bar strengths. This result is valid for bars of all evolutionary stages, which are embedded within galaxies of all stellar masses. More generally, this analysis reinforces the importance of not azimuthally averaging spatially resolved data when non-axisymmetric galaxy components are present, lest subtle details be washed out.

5 SUMMARY AND FUTURE WORK

We have investigated gradients in the spatially resolved stellar populations of strongly barred galaxies in the MaNGA galaxy survey via full spectral fitting and absorption line population indicators. By separating spaxels dominated by bar light, and comparing to those within disc regions at the same radii for the first time in a large sample of galaxies, we find that

(i) The stellar age and metallicity gradients as inferred from index measurements of $H\beta$ and $[MgFe]$ and STARLIGHT full spectrum fits in the barred regions of barred galaxies are flatter than within the disc region. From this, we conclude we have robust observational evidence of bars radially mixing material at all stages of bar evolution in local Universe galaxies.

(ii) We confirm that individual structures within galaxies can comprise different distributions of stellar populations, and that one should not azimuthally average IFU data with non-axisymmetric structures within them as averaging loses important structural information.

Future work will involve examining how the stellar age and metallicity changes as a function of radius in barred and non-barred galaxies. We will compare this with simulations to determine how bars evolve within galaxies and the time-scales involved in bar dynamics.

ACKNOWLEDGEMENTS

The authors wish to thank the anonymous referee, whose comments improved the quality of this manuscript. JHK acknowledges financial support from the European Union's Horizon 2020 research and innovation programme under Marie Skłodowska-Curie grant agreement no. 721463 to the SUNDIAL ITN network, from the Spanish Ministry of Economy and Competitiveness (MINECO) under grant agreement no. AYA2016-76219-P, from the Fundación BBVA under its 2017 programme of assistance to scientific research groups, for the project 'Using machine-learning techniques to drag galaxies from the noise in deep imaging', and from the Leverhulme Trust through the award of a Visiting Professorship at LJMU. RR thanks CNPq and FAPERGS for financial support. Funding for the Sloan Digital Sky Survey IV has been provided by the $\langle 0:funding-source \rangle$ Alfred P. Sloan Foundation $\langle 0:funding-source \rangle$, the U.S. Department of Energy Office of Science, and the Participating Institutions. SDSS-IV acknowledges support and resources from the Center for High-

Performance Computing at the University of Utah. The SDSS web site is www.sdss.org.

SDSS-IV is managed by the Astrophysical Research Consortium for the Participating Institutions of the SDSS Collaboration including the Brazilian Participation Group, the Carnegie Institution for Science, Carnegie Mellon University, the Chilean Participation Group, the French Participation Group, Harvard-Smithsonian Center for Astrophysics, Instituto de Astrofísica de Canarias, The Johns Hopkins University, Kavli Institute for the Physics and Mathematics of the Universe (IPMU) / University of Tokyo, Lawrence Berkeley National Laboratory, Leibniz Institut für Astrophysik Potsdam (AIP), Max-Planck-Institut für Astronomie (MPIA Heidelberg), Max-Planck-Institut für Astrophysik (MPA Garching), Max-Planck-Institut für Extraterrestrische Physik (MPE), National Astronomical Observatories of China, New Mexico State University, New York University, University of Notre Dame, Observatório Nacional / MCTI, The Ohio State University, Pennsylvania State University, Shanghai Astronomical Observatory, United Kingdom Participation Group, Universidad Nacional Autónoma de México, University of Arizona, University of Colorado Boulder, University of Oxford, University of Portsmouth, University of Utah, University of Virginia, University of Washington, University of Wisconsin, Vanderbilt University, and Yale University.

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